

$\frac{1 \quad 0}{\alpha \wedge \beta}$	$\frac{1 \quad 0}{\alpha \wedge \beta}$	$\frac{1 \quad 0}{\alpha \vee \beta}$	$\frac{1 \quad 0}{\alpha \vee \beta}$
$\alpha$	#1: $\alpha$	#1: $\alpha$	$\alpha$
$\beta$	#2: $\beta$	#2: $\beta$	$\beta$

$\frac{1 \quad 0}{\alpha \rightarrow \beta}$	$\frac{1 \quad 0}{\alpha \rightarrow \beta}$	$\frac{1 \quad 0}{\sim \alpha}$	$\frac{1 \quad 0}{\sim \alpha}$
#1: $\alpha$			
#2: $\beta$			

$\downarrow$  (introduce a new world)       $\downarrow$

$\frac{1 \quad 0}{\alpha \quad \beta}$	$\frac{1 \quad 0}{\alpha}$
$\star$	$\star$

1. Show that the formulas below are intuitionistic tautologies.

- $p \rightarrow p$
- $p \rightarrow \sim \sim p$  (What about  $\sim \sim p \rightarrow p$ ?)
- $\sim p \rightarrow \sim \sim \sim p$

2. Using the method of analytic tables, decide whether the following formulas are intuitionistic tautologies.

- (a)  $p \vee \sim p$
- (b)  $p \rightarrow \sim \sim p$
- (c)  $\sim \sim p \rightarrow p$
- (d)  $(p \rightarrow q) \vee (q \rightarrow p)$
- (e)  $q \vee (q \rightarrow (p \vee \sim p))$