

From the lectures:

$$\begin{array}{ccc} \phi \models_{int} \psi & \iff & \models_{int} \phi \rightarrow \psi \\ \phi \models_{int} \psi, \sim\psi & \iff & \models_{int} \sim\phi \end{array}$$

Decide whether the following statements hold.

1. $\sim\alpha \rightarrow \beta, \sim\alpha \rightarrow \sim\beta \models_{int} \alpha$
 2. $\sim\alpha \rightarrow \beta, \sim\alpha \rightarrow \sim\beta \models_{int} \sim\sim\alpha$
 3. $\alpha \rightarrow \beta, \alpha \rightarrow \gamma \models_{int} \alpha \rightarrow (\beta \wedge \gamma)$
 4. $\alpha \rightarrow \gamma, \beta \rightarrow \gamma \models_{int} (\alpha \vee \beta) \rightarrow \gamma$
 5. $\alpha \rightarrow \beta \models_{int} \sim(\alpha \wedge \sim\beta)$
 6. $\sim(\alpha \wedge \sim\beta) \models_{int} \alpha \rightarrow \beta$
 7. $\alpha \rightarrow (\alpha \rightarrow \beta) \models_{int} \alpha \rightarrow \beta$
 8. $\alpha \rightarrow (\beta \rightarrow \gamma) \models_{int} \beta \rightarrow (\alpha \rightarrow \gamma)$
 9. $\sim(\alpha \rightarrow \sim\beta) \models_{int} \alpha \wedge \beta$
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$\frac{}{\alpha \wedge \beta}$	$\frac{1 \quad 0}{\alpha \wedge \beta}$	$\frac{1 \quad 0}{\alpha \vee \beta}$	$\frac{1 \quad 0}{\alpha \vee \beta}$
α	$\#1: \quad \alpha$	$\#1: \quad \alpha$	α
β	$\#2: \quad \beta$	$\#2: \quad \beta$	β

$\frac{1 \quad 0}{\alpha \rightarrow \beta}$	$\frac{1 \quad 0}{\alpha \rightarrow \beta}$	$\frac{1 \quad 0}{\sim\alpha}$	$\frac{1 \quad 0}{\sim\alpha}$
$\#1: \quad \alpha$	\star	α	\star
$\#2: \quad \beta$	↓ (introduce a new world)		↓
	$\frac{1 \quad 0}{\alpha \quad \beta}$		
	α	β	\star
	\star		